# Jeffrey D. Carlson (he/him)

	jeffrey.carlson@tufts.edu	
Positions	Universidade Estadual de Campinas (UNICAMP) (April 2024–May 2024)	
	Visiting scholarship	
	Tufts University (January 2023–August 2023)	
	Visiting scholarship	
	Imperial College London (January 2021–December 2022)	
	Research fellowship	
	Fields Institute (Spring 2020)	
	loint postdoctoral followship	
	University of Terente (2016, 2010)	
	Postdoctoral fellowshin	
	Pác Deuterado de Excelôncia	
	funded through IMPA (o Instituto Nacional de Matemática Pura e Aplicada)	
	and CAPES (a Coordenação de Aperfeiçoamento de Pessoal de Nível Superior)	
Education	Tufts University	
	Ph.D. in Mathematics (2015)	
	Advisor: Loring W. Tu	
	Dissertation: On the equivariant conomology of nomogeneous spaces	
Citizenship	United States	
Interests	Equivariant topology: cobordism, K-theory, and Borel cohomology	
	Topology and geometry of group actions on manifolds	
	$A_{\infty}$ -algebras	
	Symplectic geometry	
	Galois cohomology	
	Low-dimensional topology and surface dynamics	
Funding	Heilbronn Focused Research Grant: Koszulity and formality in Galois cohomology	
Invited research visits	National Center for Theoretical Sciences at National Taiwan University (April-May 2017)	
Selected invited	[To be announced],	
conference talks	Workshop on Toric Topology, Fields Institute, Toronto (Aug. 2024)	
	<i>The topology of Gelfand–Zeitlin fibers</i> , Workshop on Lie Groups, Singular Spaces, and Higher Structures, <b>Fields Institute, Toronto</b> (Jan. 2023)	
	The topology of Gelfand–Zeitlin fibers,	
	AMS Special Session on Integrable Systems and Symplectic Group Actions,	
	The topology of Colland Zoitlin fibers	
	Gone Fishing 2020–2022, Georgia Southern University, Savannah, Georgia /online (Apr. 2022)	
	Multiplicative collapse in the Eilenberg–Moore spectral sequence,	
	Transpennine Topology Triangle, UK/online (Dec. 2020)	

#### The cohomology of Gelfand–Zeitlin fibers,

International Conference: Topology and Geometry of Group Actions, Higher School of Economics, Moscow/online (Nov. 2020)

Realization of torus representations as fixed-point data, Workshop on Polyhedral Products in Homotopy Theory, Fields Institute, Toronto (Jan. 2020)

Local integration in equivariant cobordism theory,

"Topology" session,

The equivariant K-theory of a cohomogeneity-one action,

"Equivariant methods in differential and algebraic geometry" session,

Canadian Mathematical Society Summer Meeting, Regina, Saskatchewan (June 2019)

Equivariant formality beyond Hamiltonian actions, Symmetries of Symplectic Manifolds and Related Topics, Mathematical Congress of the Americas, Montreal (July 2017)

*Equivariant formality in rational cohomology and K-theory*, Conference on Geometry in Algebra and Algebra in Geometry, **Universidade de São Paulo** (Nov. 2015)

Selected invited seminar talks

A topologia da fibra de Gelfand–Zeitlin, Seminário de Geometria, Universidade Estadual de Campinas (Unicamp), SP, Brazil (May 2024)

Biquotients and a product on the two-sided bar construction,

International Polyhedral Products Seminar, Princeton/online (Oct. 2023)

Products on Tor, Algebraic topology seminar, **University of Warwick** (Mar. 2023)

The topology of Gelfand–Zeitlin fibers, Interactions between symplectic geometry, combinatorics, and number theory seminar, Universität zu Köln/Philipps-Universität Marburg/online (Nov. 2022)

The topology of Gelfand–Zeitlin fibers, Topology seminar, Heinrich-Heine-**Universität Düsseldorf** (Oct. 2022)

Equivariant formality of isotropy actions and products of spheres, Geometry, topology, and group theory seminar, Westfälische Wilhelms-**Universität Münster** (Oct. 2022)

The topology of the Gelfand–Zeitlin fiber, International Polyhedral Products Seminar, **Princeton**/online (Apr. 2022)

The topology of the Gelfand–Zeitlin fiber, Symplectic Monday, **IBS Center for Geometry and Physics, Pohang, Korea**/online (Dec. 2021)

*The topology of the Gelfand–Zeitlin fiber,* London Geometry and Topology Seminar, **Imperial College London** (Dec. 2021)

*Products on Tor, homogeneous spaces, and Borel cohomology,* Topology seminar, **University of Rochester**/online (Nov. 2021)

*The topology of the Gelfand–Zeitlin fiber*, Differential geometry and topology seminar, **University of Cambridge** (Nov. 2021)

Biquotients and a product on the two-sided bar construction, Algebraic topology seminar, Universidad Nacional Autónoma de México/online (May 2021)

*Multiplicative collapse in the Eilenberg–Moore spectral sequence*, Algebraic topology seminar, **University of Michigan**/online (Apr. 2021)

The K-theory of an isotropy action and an unsolved problem in polynomial rings (in Portuguese), Seminário Salomônico, **Universidade Federal Fluminense, Niterói, RJ, Brazil** (August 2019)

Equivariant formality, K-theory, and isotropy,

#### Topology seminar, University of Rochester (October 2018)

Cohomogeneity-one actions and a little-remarked structure on the Mayer–Vietoris sequence, Symplectic seminar, **University of Toronto** (March 2017)

*Equivariant formality in rational cohomology and K-theory,* Geometry and topology seminar, **Western University, London, ON, Canada** (December 2016)

*Equivariant formality of isotropy actions in rationalized cohomology and K-theory*, Seminário de física matemática, **IMPA**, **Rio de Janeiro** (May 2016)

# Products on Tor,

Algebraic Topology, in Memory of Hans-Joachim Baues, Max Planck Institute for Mathematics, Bonn (Oct. 2022)

*Products on Tor, homogeneous spaces, and Borel cohomology,* Algebraic structures in topology, **San Juan, Puerto Rico** (May–June 2022)

*Realization of fixed-point data for locally standard torus actions*, Glances@Manifolds, **Jagiellonian University**, **Kraków** (July 2018)

The equivariant cohomology and K-theory of a cohomogeneity-one action,

Algebraic Topology, Combinatorics, and Mathematical Physics, on the occasion of Victor Buchstaber's 75th birthday, **Steklov Institute** and **Skolkovo Technical Institute**, **Moscow** (May 2018)

Formality and equivariant formality for isotropy actions (in Portuguese), XX Encontro Brasileiro de Topologia,

Universidade Tecnológica Federal do Paraná, Curitiba, PR, Brazil (July 2016)

## Teaching

Some contributed

talks in colorful

locations

# Course coordinator and lecturer,

- · Commutative Algebra (Imperial College London),
- · Vector Calculus (University of Toronto, four semesters, supervising an undergraduate TA),
- Mathematics of Social Choice (Tufts University)

# Seminar coordinator and lecturer,

- Formality (Western University),
- Equivariant Cohomology (Universidade de São Paulo)

#### Lecturer,

- · Calculus (University of Toronto & Tufts University, three semesters),
- Finite Mathematics (Tufts University)

## Reading group facilitator,

- Foundations of Algebraic Geometry (Western University) (mentor, Directed Reading Program in Mathematics),
- Topologia Diferencial (Universidade de São Paulo)

#### Teaching assistant (all at Tufts University),

- · Differential Forms in Algebraic Topology,
- · Mathematical Neuroscience,
- History of Mathematics,
- Number Theory,
- Complex Analysis,
- · Real Analysis I & II

Tutor for eight students, ranging from Year 1 to M.S. (Imperial College London, 2021–2022)

Fellow of the Graduate Institute for Teaching (Tufts University, Summer 2010)

Service

Referee, Proc. London Math. Soc. Trans. Amer. Math. Soc., J. Topol., Math. Z., São Paulo J. Math. Sciences, J. Topol. Anal., Homology, Homotopy Appl., Comtemp. Math.

My version of refereeing involves following through and verifying every detail of each argument, generates several pages of commentary, and requires at least a week for a first pass, with less time spent on each subsequent revision.

Quick opinions, Trans. Amer. Math. Soc., J. Reine Angew. Math., J. Lie Theory

Master's defense committee member, Tufts University, for Kevin Woytowich, 25 Apr. 2023

Organizer, Special Session on Equivariant Cohomology, AMS Spring Eastern Virtual Sectional Meeting (2022, with Loring W. Tu)

> "Equivariant geometry and topology" session, CMS Winter Meeting, Niagara, Ontario (2016, with Elisheva Adina Gamse).

Reviewer, Mathematical Reviews.

## Editorial board, Poincaré Institute for Mathematics Education, Summer 2013

The Poincaré Institute is an NSF-funded collaboration between Tufts University and the non-profit Technical Education Research Centers designed to improve middle school mathematics education through graduate-level online courses offered to in-service middle school mathematics teachers.

#### (Copy)edited books and articles

I often provided feedback on papers and particularly texts I read. My approach is rather thorough and sometimes leads to what I like to consider significant improvement. For example, Prof. Tu had this to say in the preface to the second edition of *An Introduction to Manifolds*:

Every author needs an audience. In preparing the second edition, I was particularly fortunate to have a loyal and devoted audience of two, George F. Leger and Jeffrey D. Carlson, who accompanied me every step of the way. Section by section, they combed through the revision and gave me detailed comments, corrections, and suggestions. In fact, the two hundred pages of feedback that Jeff wrote was in itself a masterpiece of criticism. Whatever clarity this book finally achieves results in a large measure from their effort.

## by Loring Tu (selected)

- Introductory Lectures on Equivariant Cohomology, Annals of Math. Studies 204, Princeton Univ. Press, Princeton, New Jersey, 2020.
- Elements of Equivariant Cohomology, with Raoul Bott, unpublished.
- Differential Forms in Algebraic Topology, 2nd edition, with Raoul Bott, edition in progress.
- Differential Geometry: Connections, Curvature, and Characteristic Classes, Grad. Texts in Math. 275, Springer, New York, 2017.
- An Introduction to Manifolds, [first and] second edition, Universitext, Springer, New York, 2011.
- Raoul Bott: Collected Papers, volume 5 [collection of permissions], Birkhäuser, Basel, 2017.
- From sheaf cohomology to the algebraic de Rham theorem (with Fouad El Zein), pp. 69–121 in *Hodge Theory*, eds. Eduardo Cattani, Fouad El Zein, Phillip A. Griffiths, and Lê Dũng Tráng, Princeton Univ. Press, Princeton, New Jersey, 2014.
- Computing characteristic numbers using fixed points, in A Celebration of the Mathematical Legacy of Raoul Bott, CRM Proceedings and Lecture Notes, vol. 50, American Mathematical Society, Providence, RI, 2010, pp. 185–206.

#### by others

- Mathematical Logic and Computation, Jeremy Avigad, Cambridge University Press, 2022.
- An Introduction to Modeling Neuronal Dynamics, Christoph Börgers, Texts in Applied Mathematics vol. 66, Springer, New York, 2017.

	<ul> <li>A Primer on Mapping Class Groups, I vol. 49, Princeton University Press, Pr</li> <li>Category Theory, Steven Awodey, Ox</li> <li>Computability and Learnability, Kevin</li> <li>An introductory text on the calculus of</li> </ul>	Benson Farb and Dan Margalit, Princeton Mathematical Serie rinceton, NJ, 2011. ford Logic Guides vol. 52, Oxford Univ. Press, New York, 2006 Kelly, unpublished. <sup>1</sup> variations, William Hrusa, unpublished.		
Languages	English: native (polished if ornate, a byproduct of formal overeducation) Portuguese: fluent at the level of the news, but not of poetry			
	Mandarin: basic conversation (but worsen	ing accent), menu comprehension		
References (research)	Loring W. Tu, Professor	James Stasheff, Professor Emeritus		
	Department of Mathematics	University of North Carolina at Chapel Hill		
	Tufts University	University of Pennsylvania		
	177 College Avenue	Department of Mathematics		
	Medford MA 02155	209 South 33rd Street		
	USA	Philadelphia, PA 19104-6395		
	loring.tu@tufts.edu	USA		
		jds@math.upenn.edu		
	Yael Karshon, Professor	Michael A. Hill, Professor		
	Department of Mathematics	Department of Mathematics		
	University of Toronto	University of California Los Angeles		
	40 St. George Street	Box 951555		
	Toronto ON M5S 2E4	Los Angeles, CA 90095-1555		
	Canada	USA		
	karshon@math.toronto.edu	mikehill@math.ucla.edu		
	Ján Mináč, Professor	Oliver Goertsches, Professor		
	Department of Mathematics	Fachbereich Mathematik und Informatik		
	Western University	Philipps-Universität Marburg		
	Middlesex College	Hans-Meerwein-Straße 6		
	London ON N6A 5B7	35032 Marburg		
	Canada	Deutschland		
	minac@uwo.ca	goertsch@mathematik.uni-marburg.de		
	Matthias Franz, Professor			
	Department of Mathematics			
	Western University			
	widalesex College			
	LUHUUH UN NOA 307 Canada			
	mfranz@uwo.ca			
References (teaching)	Kim Ruane, Professor and Chair	Ilia Binder, Professor		
-	Department of Mathematics	Department of Mathematics		
	Tufts University	University of Toronto		
	177 College Avenue	40 St. George Street		
	Medford MA 02155	Toronto ON M5S 2E4		
	USA	Canada		
	kim muono@tufta_odu	ilia@math_tamanta_adu		

Books	1.	The Rational Cohomology of Homogeneous Spaces (under revision for Springer's Developments in Mathe	jdkcarlson.github.io/homog_book.pdf <i>matics</i> series, 155pp., 2018).		
	2.	2. Solutions to Introduction to Commutative Algebra by Atiyah–MacDonald			
		(2011, revised 2021, 134pp.) jdkcarlso	on.github.io/intro_comm_alg(2021).pdf		
Preprints	1.	Products on Tor (submitted, 2022, 23pp.)	arxiv.org/abs/2311.16007		
	2.	A ring structure on Tor ( <b>under revision for <i>Forum Math. Sigma</i></b> , 2022, 44pp.)	arxiv.org/abs/2306.04860		
	3.	The topology of Gelfand–Zetilin fibers (submitted, 2021, 39pp., with Jeremy Lane)	arxiv.org/abs/2107.02721		
	4.	Fixed points and semifree bordism (submitted, 2019, 13pp.)	arxiv.org/abs/1908.06906		
	5.	The K-theory of cohomogeneity-one actions (under revision for <i>Adv. Math.</i> , 2018, 40pp.)	arxiv.org/abs/1805.00502		
	6.	Realization of abstract GKM isotropy data (2016–, with Elisheva Adina Gamse and Yael Karshon)	jdkcarlson.github.io/realization.pdf		
	7.	Commensurability of two-multitwist pseudo-Anosovs (2010, 33pp.)	arxiv.org/abs/1011.0247		
Publications		1. The cohomology of homogeneous spaces in historical context (to be published in Contemp. Math. volume Group Actions and Equivariant Cohomology, 2023, 33pp.)			
	2.	Equivariant formality of corank-one isotropy actions and products of rational spheres ( <i>Math. Z.</i> , 2023, 45pp., with Chen He)	arxiv.org/abs/2204.00135		
	3.	The cohomology of biquotients via a product on the two-sided bar construction (to be published in <i>Algebr Geom Topol</i> 2020 48pp	arxiv.org/abs/2106.02986		
	4.	K-theory and formality ( <i>Int. Math. Res. Not.</i> , 2022, 46pp.)	arxiv.org/abs/1810.09685		
	5.	Grassmannians and the equivariant cohomology of isotro ( <i>Proc. Amer. Math. Soc.</i> , 2021, 15pp.)	by actions arxiv.org/abs/1611.01175		
	6.	The K-theory of the conjugation action ( <i>C. R. Math. Acad. Sci., Paris</i> , 2021, 2pp.)	arxiv.org/abs/2312.00049		
	7.	The equivariant cohomology ring of a cohomogeneity-one ( <i>Geom. Dedicata</i> , 2019, 18pp., with Chen He, Oliver Goe	action arxiv.org/abs/1802.02304 ertsches, and Liviu Mare)		
	8.	Equivariant formality of homogeneous spaces ( <i>J. London Math. Soc.</i> , 2018, 23pp., with Chi-Kwong Fol	arxiv.org/abs/1511.06228		
	9.	Equivariant formality of isotropic torus actions ( <i>J. Homotopy and Relat. Struct.</i> , 2018, 34pp.)	arxiv.org/abs/1410.5740		
	10.	Conceptions of topological transitivity ( <i>Topology AppI</i> , 2012, 15pp., with Ethan Akin)	arxiv.org/abs/1108.4710		